

REGRESNÁ A KORELAČNÁ ANALÝZA

$$\text{I. } \sum_{i=1}^n y_i = nb_0 + b_1 \sum_{i=1}^n x_i$$

$$\text{II. } b_1 = \frac{\text{cov } xy}{s_x^2}$$

$$\sum_{i=1}^n y_i x_i = b_0 \sum_{i=1}^n x_i + b_1 \sum_{i=1}^n x_i^2$$

$$b_0 = \bar{y} - b_1 \bar{x}$$

$$F = \frac{MSM}{MSR} = \frac{\frac{SSM}{1}}{\frac{SSR}{n-2}} = \frac{(n-2) \sum_{i=1}^n (\hat{y}_i - \bar{y})^2}{\sum_{i=1}^n (y_i - \hat{y}_i)^2} \quad F > F_{1-\alpha}(1, n-2)$$

Rozptyl	Interval spoľahlivosti
$s_{rez}^2 = MSR = \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n-2}$	_____
$s_{b_1}^2 = \frac{s_{rez}^2}{\sum_{i=1}^n (x_i - \bar{x})^2}$	$P(b_1 - t_{\frac{1-\alpha}{2}} s_{b_1} < \beta_1 < b_1 + t_{\frac{1-\alpha}{2}} s_{b_1}) = 1 - \alpha$
$s_{\hat{y}_0}^2 = s_{rez}^2 \left[\frac{1}{n} + \frac{(x_0 - \bar{x})^2}{\sum_{i=1}^n (x_i - \bar{x})^2} \right]$	$P(\hat{y}_0 - t_{\frac{1-\alpha}{2}} \cdot s_{\hat{y}_0} < \mu_{Y/x_0} < \hat{y}_0 + t_{\frac{1-\alpha}{2}} \cdot s_{\hat{y}_0}) = 1 - \alpha$
$s_{y_0}^2 = s_{\hat{y}_0}^2 + s_{rez}^2$	$P(\hat{y}_0 - t_{\frac{1-\alpha}{2}} \cdot s_{y_0} < Y_{x_0} < \hat{y}_0 + t_{\frac{1-\alpha}{2}} \cdot s_{y_0}) = 1 - \alpha$

Nulová hypotéza	Alternatívna hypotéza	Testovacia charakteristika	Kritická oblast'
$H_0: \beta_1 = \beta_{10}$	$H_1: \beta_1 \neq \beta_{10}$	$t = \frac{b_1 - \beta_{10}}{s_{b_1}}$	$ t > t_{\frac{1-\alpha}{2}}(n-2)$
$H_0: \beta_1 = 0$	$H_1: \beta_1 \neq 0$	$t = \frac{b_1}{s_{b_1}}$	$ t > t_{\frac{1-\alpha}{2}}(n-2)$
$H_0: \beta_{11} = \beta_{12}$	$H_1: \beta_{11} \neq \beta_{12}$	$t = \frac{b_{11} - b_{12}}{s_{b_{11}-b_{12}}}$	$ t > t_{\frac{1-\alpha}{2}}(n_1 + n_2 - 4)$
$H_0: \rho = \rho_0$	$H_1: \rho \neq \rho_0$	$z = (z_F - z_{F_0}) \sqrt{n-3}$	$ z > z_{\frac{1-\alpha}{2}}$
$H_0: \rho = 0$	$H_1: \rho \neq 0$	$z = z_F \sqrt{n-3}$	$ z > z_{\frac{1-\alpha}{2}}$
		$t = \frac{r}{\sqrt{1-r^2}} \sqrt{n-2}$	$ t > t_{\frac{1-\alpha}{2}(n-2)}$
		$F = \frac{(n-2)r^2}{1-r^2}$	$F > F_{1-\alpha(1,n-2)}$
$H_0: \rho_1 = \rho_2$	$H_1: \rho_1 \neq \rho_2$	$z = \frac{(z_{F_1} - z_{F_2})}{\sqrt{\frac{1}{n_1-3} + \frac{1}{n_2-3}}}$	$ z > z_{\frac{1-\alpha}{2}}$

$$s_{b_{11}-b_{12}}^2 = s^2 \cdot \left[\frac{1}{\sum_{i=1}^{n_1} (x_{i1} - \bar{x}_1)^2} + \frac{1}{\sum_{i=1}^{n_2} (x_{i2} - \bar{x}_2)^2} \right]$$

$$s^2 = \frac{(n_1-2).s_{rez1}^2 + (n_2-2).s_{rez2}^2}{n_1 + n_2 - 4}$$

$$r_{xy}=\frac{\text{cov}\, xy}{s_xs_y}\,,\quad r_{xy}=b_1\frac{s_x}{s_y}\,,\quad \left|r_{xy}\right|=\sqrt{a_1b_1}\,,\quad r_{xy}^2=\frac{SSM}{SST}=1-\frac{SSR}{SST}\,,\quad r_{adj}^2=1-(1-r_{xy}^2)\frac{n-1}{n-2}$$

$$P(z_F-z_{_{1-\frac{\alpha}{2}}}\frac{1}{\sqrt{n-3}} < Z_F < z_F + z_{_{1-\frac{\alpha}{2}}}\frac{1}{\sqrt{n-3}}) = 1 - \alpha$$

$$\chi^2 = \sum_{j=1}^s \sum_{i=1}^r \frac{(O_{ij}-E_{ij})^2}{E_{ij}} \qquad \qquad \chi^2 > \chi^2_{1-\alpha} \big[(r-1).(s-1) \big]$$

$$Q_{_{AB}}=\frac{(ab).(\alpha.\beta)-(a\beta).(ab)}{(ab).(\alpha.\beta)+(a\beta).(ab)}\,,\; R_{_{AB}}=\frac{n(ab)-(a).(b)}{\sqrt{(a).(b).(\alpha).(\beta)}}\,,\; C=\sqrt{\frac{\chi^2}{n+\chi^2}}\,,\;\tau^2=\frac{\phi^2}{\sqrt{(r-1).(s-1)}}\,,\; V=\sqrt{\frac{\chi^2}{n.h}}$$

ČASOVÉ RADY

$$\overline{y}_{ch}=\frac{\frac{y_1}{2}+y_2+...+y_{T-1}+\frac{y_T}{2}}{T-1}\qquad\qquad\qquad\overline{y}_{ch}=\frac{\frac{y_1+y_2}{2}v_2+\frac{y_2+y_3}{2}v_3+....+\frac{y_{T-1}+y_T}{2}v_T}{v_2+v_3+...+v_T}$$

$$\boxed{\begin{array}{l} \sum\limits_{t=1}^Ty_t=T~b_0+b_1\sum\limits_{t=1}^Tt \\ \sum\limits_{t=1}^Tt~y_t=b_0\sum\limits_{t=1}^Tt+b_1\sum\limits_{t=1}^Tt^2 \end{array}} \qquad \boxed{\begin{array}{l} \sum\limits_{t=1}^Ty_t=Tb_0+b_1\sum\limits_{t=1}^Tt+b_2\sum\limits_{t=1}^Tt^2 \\ \sum\limits_{t=1}^Ty_t=b_0\sum\limits_{t=1}^Tt+b_1\sum\limits_{t=1}^Tt^2+b_2\sum\limits_{t=1}^Tt^3 \\ \sum\limits_{t=1}^Tt^2y_t=b_0\sum\limits_{t=1}^Tt^2+b_1\sum\limits_{t=1}^Tt^3+b_2\sum\limits_{t=1}^Tt^4 \end{array}}$$

INDEXY

$$i_{pz}=\frac{\sum p_1\cdot q_1}{\sum q_1} \qquad \qquad i_{sz(0)}=\frac{\sum p_1\cdot q_0}{\sum q_0} \qquad \qquad i_{\check s(1)}=\frac{\sum p_1\cdot q_1}{\sum q_0}\\$$

$$i_{pz}=i_{sz(0)}\cdot i_{\check s(1)}=i_{sz(1)}\cdot i_{\check s(0)}$$

$$\Delta_{pz}=\Delta_{sz(0)}+\Delta_{\check s(1)}=\Delta_{sz(1)}+\Delta_{\check s(0)}$$

$$I_Q=\frac{\sum p_1\cdot q_1}{\sum p_0\cdot q_0}=\frac{\sum Q_1}{\sum Q_0} \qquad I_{p(0)}=\frac{\sum p_1\cdot q_0}{\sum p_0\cdot q_0}=\frac{\sum \frac{p_1}{p_0}\cdot Q_0}{\sum Q_0} \qquad I_{q(1)}=\frac{\sum p_1\cdot q_1}{\sum p_1\cdot q_0}=\frac{\sum Q_1}{\sum \frac{q_1}{q_0}}$$

$$I_Q=I_{p(0)}\cdot I_{q(1)}=I_{p(1)}\cdot I_{q(0)}$$

$$\Delta_Q=\Delta_{p(0)}+\Delta_{q(1)}=\Delta_{p(1)}+\Delta_{q(0)}$$